# DRAFT

# Geometry EOC Test Item Specifications

INTENDED FOR TEST ITEM WRITERS AND REVIEWERS FOR FLORIDA'S STATEWIDE ASSESSMENTS. NOT FOR INSTRUCTIONAL USE. The contents of these draft *Test Item Specifications (Specifications)* are based on the benchmarks provided in Florida's Benchmarks for Excellent Student Thinking (B.E.S.T.) Standards. The *Specifications* define the content and format of the tests and test items and indicate the alignment of items with the benchmarks for test item writers and reviewers. The *Specifications* are not intended for instructional use.

With the adoption of Florida's B.E.S.T. Standards for ELA and Mathematics, the following comprehensive resource has been developed to support educators.

• Within the standards, **benchmark clarifications** provide helpful information for educators to understand and implement each standard.

Given the availability of B.E.S.T. resources and to prevent any misuse of the *Specifications* by educators, item specifications for ELA and Mathematics assessments aligned to the B.E.S.T. Standards will be reserved for their intended purpose of guiding item writers and reviewers. B.E.S.T. Standards implementation should be driven by the instructional support provided by the Just Read, Florida! (JRF) Office and the Bureau of Standards and Instructional Support (BSIS) to ensure that the focus remains on the content and skills students will engage with in the classroom.

### Origin of the Specifications

The Florida Department of Education convened committees of Florida educators to help develop and approve the specifications documents.

#### **Item Type Descriptions**

The Florida B.E.S.T. Standards Assessments are composed of test items that include traditional multiple-choice items as well as technology-enhanced items that require students to select and/or support their answers.

The various item types are described below.

- Technology-Enhanced Item Types—Mathematics
  - Editing Task Choice—The student clicks a drop-down menu containing options to complete an equation or expression, a statement, or other component. The student then selects the correct response from the drop-down menu. For paper-based assessments, this item type is modified; the student fills in a bubble to indicate a selection.
  - Selectable Hot Text—The student is directed to click on one or more correct answers from among a number of options. When the student hovers over the options (e.g., phrases, sentences, numbers, or expressions), the text will highlight. This indicates that the text is selectable ("hot"). The options may be presented in various ways (e.g., as a list, embedded within text, or in a table). The student can then click on an option to select it. For paper-based assessments, this item type is modified; the student fills in a bubble to indicate a selection.
  - **Multiselect**—The student is directed to select all the correct answers from among a number of options. These items are different from Multiple Choice items, which allow the student to select only one correct answer. These items appear in the online and paper-based assessments.
  - Graphic Response Item Display (GRID) The student uses the point, line, or arrow tools to create a response on a graph. The item type may also require the student to select numbers, words, phrases, or images and use the drag-and-drop feature to place them into a graphic. For paper-based assessments, this item type will be replaced with another item type.
  - Equation Editor—The student enters a number, variable, expression, or equation, as appropriate to the test item, in a response box. The student is presented with a toolbar that includes a variety of mathematical symbols that can be used to create a response. The response box may be separate from the text of the item, or it may be embedded within text of the item (e.g., in line with a sentence or within a table). For paper-based assessments, this item type is modified; the student writes a response in the response box.
  - Matching Item—The student checks a box to indicate whether information from a column header matches information from a row. The number of correct answer options per row or column may vary. These items appear in the online and paper-based assessments.

Any of the item types may be combined into a single item with multiple parts called a multi-interaction item. The student will interact with different item types within a single item. Each part could be a different item type. For paper-based assessments, different item types (multiple choice, multiselect, editing task choice, selectable hot text, matching, and equation editor) may be combined into a single item.

### **Item Specifications Definitions**

- Assessment Limits define the range of content knowledge and degree of difficulty that should be assessed in the assessment items for the benchmark(s).
- Also Assesses—Where mastery of overlapping mathematical skills of associated benchmark(s) could be assessed through primary benchmark(s).

### • Calculator Availability

The following chart displays the type of calculator available for each grade or course B.E.S.T. Assessment. Note: For grades 6, 7, 8, Algebra 1, and Geometry, calculators are available for the entire assessment.

Grade/Course	Calculator
3, 4, 5	None
6	Four-function
7,8	Desmos scientific
Algebra 1, Geometry	Desmos scientific

#### • Calculator Designations

- None—Items for this benchmark may not allow for the availability of a calculator.
- Available—Items for this benchmark **must** allow for the availability of a calculator.

#### • Context Designations

Any item could include justifying and error analysis through reasoning.

- **Real-world**—authentic application of mathematics to real-world situations
- **Mathematical**—using models, equations, or evaluation of mathematical reasoning in the absence of a real-world context
- **Both**—Items could either use a real-world context or be strictly mathematical.

# Logic, Relationships, and Theorems

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.1	Prove relationships and theorems about lines and angles. Solve
	mathematical and real-world problems involving postulates,
	relationships and theorems of lines and angles.
Benchmark	<i>Clarification 1:</i> Postulates, relationships and theorems include vertical
Clarifications	angles are congruent; when a transversal crosses parallel lines, the
	consecutive angles are supplementary and alternate (interior and
	exterior) angles and corresponding angles are congruent; points on a
	perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.
	<i>Clarification 2:</i> Instruction includes constructing two-column proofs,
	pictorial proofs, paragraph and narrative proofs, flow chart proofs or
	informal proofs.
	<i>Clarification 3:</i> Instruction focuses on helping a student choose a
	method they can use reliably.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess postulates, relationships, and theorems beyond
	Clarification 1.
	Items requiring the student to solve problems involving vertical angles
	must include real-world context and/or the use of multiple angle
	relationships.
	Items will not require the student to identify a reason using/recognizing
	the formal name of a theorem/postulate/relationship unless
	referenced in the benchmark or clarifications.
	Items may include multiple sets of lines and angles.

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.2	Prove triangle congruence or similarity using Side-Side-Side, Side-Angle-
	Side, Angle-Side-Angle, Angle-Angle-Side, Angle-Angle and Hypotenuse-
	Leg.
Benchmark	Clarification 1: Instruction includes constructing two-column proofs,
Clarifications	pictorial proofs, paragraph and narrative proofs, flow chart proofs or
	informal proofs.
	Clarification 2: Instruction focuses on helping a student choose a
	method they can use reliably.
Context	Mathematical
Calculator	Available
Assessment Limits	Items will not require the student to identify a reason using/recognizing
	the formal name of a theorem/postulate/relationship unless
	referenced in the benchmark or clarifications.

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.3	Prove relationships and theorems about triangles. Solve mathematical
	and real-world problems involving postulates, relationships and
	theorems of triangles.
Benchmark	<i>Clarification 1:</i> Postulates, relationships and theorems include measures
Clarifications	angles of a triangle sum to 360°; triangle inequality theorem; base
	angles of isosceles triangles are congruent; the segment joining
	midpoints of two sides of a triangle is parallel to the third side and half
	the length; the medians of a triangle meet at a point.
	<i>Clarification 2:</i> Instruction includes constructing two-column proofs,
	pictorial proofs, paragraph and narrative proofs, flow chart proofs or
	informal proofs.
	Clarification 3: Instruction focuses on helping a student choose a
	method they can use reliably.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess postulates, relationships, and theorems beyond Clarification 1.
	Items may use geometric figures of any shape if the figure can be
	decomposed into a triangle or triangles.
	Items will not require the student to identify a reason using/recognizing
	the formal name of a theorem/postulate/relationship unless
	referenced in the benchmark or clarifications.
	Other than the triangle inequality theorem, items requiring the student
	to identify a reason will not require the student to recognize the
	formal name of theorems or postulates.

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.4	Prove relationships and theorems about parallelograms. Solve
	mathematical and real-world problems involving postulates,
	relationships and theorems of parallelograms.
Benchmark	<i>Clarification 1:</i> Postulates, relationships and theorems include opposite
Clarifications	sides are congruent, consecutive angles are supplementary, opposite
	angles are congruent, the diagonals of a parallelogram bisect each
	other, and rectangles are parallelograms with congruent diagonals.
	Clarification 2: Instruction includes constructing two-column proofs,
	pictorial proofs, paragraph and narrative proofs, flow chart proofs or
	informal proofs.
	Clarification 3: Instruction focuses on helping a student choose a
	method they can use reliably.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess postulates, relationships, and theorems beyond
	Clarification 1.
	Items will not require the student to identify a reason using/recognizing
	the formal name of a theorem/postulate/relationship unless
	referenced in the benchmark or clarifications.

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.5	Prove relationships and theorems about trapezoids. Solve mathematical
	theorems of trapezoids.
Benchmark	Clarification 1: Postulates, relationships and theorems include the
Clarifications	Trapezoid Midsegment Theorem and for isosceles trapezoids: base
	angles are congruent, opposite angles are supplementary and diagonals
	are congruent.
	Clarification 2: Instruction includes constructing two-column proofs,
	pictorial proofs, paragraph and narrative proofs, flow chart proofs or
	informal proofs.
	Clarification 3: Instruction focuses on helping a student choose a
	method they can use reliably.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess postulates, relationships, and theorems beyond
	Clarification 1.
	Items will not require the student to identify a reason using/recognizing
	the formal name of a theorem/postulate/relationship unless
	referenced in the benchmark or clarifications.

MA.912.GR.6	Use properties and theorems related to circles.
MA.912.GR.6.1	Solve mathematical and real-world problems involving the length of a
	secant, tangent, segment or chord in a given circle.
Benchmark	Clarification 1: Problems include relationships between two chords; two
Clarifications	secants; a secant and a tangent; and the length of the tangent from a
	point to a circle.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess relationships beyond Clarification 1.
	Angle measures will be in degrees.

MA.912.GR.6	Use properties and theorems related to circles.
MA.912.GR.6.2	Solve mathematical and real-world problems involving the measures of
	arcs and related angles.
Benchmark	Clarification 1: Within the Geometry course, problems are limited to
Clarifications	relationships between inscribed angles; central angles; and angles
	formed by the following intersections: a tangent and a secant through
	the center, two tangents, and a chord and its perpendicular bisector.
Context	Both
Calculator	Available
Assessment Limits	Angle measures will be in degrees.

MA.912.GR.6	Use properties and theorems related to circles.
MA.912.GR.6.3	Solve mathematical problems involving triangles and quadrilaterals
	inscribed in a circle.
Benchmark	Clarification 1: Instruction includes cases in which a triangle inscribed in
Clarifications	a circle has a side that is the diameter.
Context	Mathematical
Calculator	Available
Assessment Limits	Angle measures will be in degrees.

MA.912.GR.6	Use properties and theorems related to circles.
MA.912.GR.6.4	Solve mathematical and real-world problems involving the arc length
	and area of a sector in a given circle.
Benchmark	Clarification 1: Instruction focuses on the conceptual understanding
Clarifications	that for a given angle measure the length of the intercepted arc is
	proportional to the radius, and for a given radius the length of the
	intercepted arc is proportional is the angle measure.
Context	Both
Calculator	Available
Assessment Limits	Angle measures will be in degrees.

MA.912.LT.4	Develop an understanding of the fundamentals of propositional logic, arguments and methods of proof.
MA.912.LT.4.3	Identify and accurately interpret "ifthen," "if and only if," "all" and
	"not" statements. Find the converse, inverse and contrapositive of a
	statement.
Benchmark	Clarification 1: Instruction focuses on recognizing the relationships
Clarifications	between an "ifthen" statement and the converse, inverse and
	contrapositive of that statement.
	<i>Clarification 2:</i> Within the Geometry course, instruction focuses on the
	connection to proofs within the course.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess truth tables.
	Statements will reference postulates, relationships, and theorems from
	MA.912.GR.1.

MA.912.LT.4	Develop an understanding of the fundamentals of propositional logic,
	arguments and methods of proof.
MA.912.LT.4.10	Judge the validity of arguments and give counterexamples to disprove
	statements.
Benchmark	<i>Clarification 1:</i> Within the Geometry course, instruction focuses on the
Clarifications	connection to proofs within the course.
Context	Both
Calculator	Available
Assessment Limits	Statements will reference postulates, relationships, and theorems from
	MA.912.GR.1.

# **Congruence, Similarity, and Constructions**

MA.912.GR.1	Prove and apply geometric theorems to solve problems.
MA.912.GR.1.6	Solve mathematical and real-world problems involving congruence or
	similarity in two-dimensional figures.
Benchmark	Clarification 1: Instruction includes demonstrating that two-dimensional
Clarifications	figures are congruent or similar based on given information.
Context	Both
Calculator	Available
Assessment Limits	Items should not give a scale factor or assess finding a scale factor
	between two similar figures.
	Items must use figures other than two triangles when assessing similar
	figures.
	Items must use closed figures when assessing congruent and/or similar
	figures.

MA.912.GR.2	Apply properties of transformations to describe congruence or similarity
MA.912.GR.2.1	Given a preimage and image, describe the transformation and represent the transformation algebraically using coordinates. <i>Example:</i> Given a triangle whose vertices have the coordinates $(-3, 4)$ , (2, 1.7) and $(-0.4, -3)$ . If this triangle is reflected across the y-axis the transformation can be described using coordinates as $(x, y) \rightarrow (-x, y)$ resulting in the image whose vertices have the coordinates $(3, 4)$ , (-2, 1.7), and $(0.4, -3)$ .
Benchmark Clarifications	Clarification 1: Instruction includes the connection of transformations to functions that take points in the plane as inputs and give other points in the plane as outputs. Clarification 2: Transformations include translations, dilations, rotations and reflections described using words or using coordinates. Clarification 3: Within the Geometry course, rotations are limited to 90°, 180° and 270° counterclockwise or clockwise about the center of rotation, and the centers of rotations and dilations are limited to the origin or a point on the figure.
Context	Mathematical
Calculator	Available
Assessment Limits	<ul> <li>Items will not assess transformations beyond <i>Clarification 2</i>.</li> <li>Items involving a reflection across a line will include the equation written in the form y = a, x = a, y = x, or y = -x, where a is an integer.</li> <li>Items will use coordinate notation having algebraic descriptors for representing transformations.</li> <li>Items will not use function notation for representing transformations.</li> <li>Items should reference an image and its pre-image and are limited to a single transformation or a sequence of two to four transformations.</li> </ul>

MA.912.GR.2	Apply properties of transformations to describe congruence or
	similarity.
MA.912.GR.2.2	Identify transformations that do or do not preserve distance.
Benchmark	<i>Clarification 1:</i> Transformations include translations, dilations, rotations
Clarifications	and reflections described using words or using coordinates.
	Clarification 2: Instruction includes recognizing that these
	transformations preserve angle measure.
Context	Mathematical
Calculator	Available
Assessment Limits	Items will not assess transformations beyond Clarification 1.

MA.912.GR.2	Apply properties of transformations to describe congruence or
	similarity.
MA.912.GR.2.3	Identify a sequence of transformations that will map a given figure onto
	itself or onto another congruent or similar figure.
Benchmark	Clarification 1: Transformations include translations, dilations, rotations
Clarifications	and reflections described using words or using coordinates.
	Clarification 2: Within the Geometry course, figures are limited to
	triangles and quadrilaterals and rotations are limited to 90°, 180° and
	270° counterclockwise or clockwise about the center of rotation.
	Clarification 3: Instruction includes the understanding that when a
	figure is mapped onto itself using a reflection, it occurs over a line of
	symmetry.
Also Assesses	
MA.912.GR.2.6	Apply rigid transformations to map one figure onto another to justify
	that the two figures are congruent.
Benchmark	Clarification 1: Instruction includes showing that the corresponding
Clarifications	sides and the corresponding angles are congruent.
MA.912.GR.2.8	Apply an appropriate transformation to map one figure onto another to
	justify that the two figures are similar.
Benchmark	Clarification 1: Instruction includes showing that the corresponding
Clarifications	sides are proportional, and the corresponding angles are congruent.
Context	Mathematical
Calculator	Available
Assessment Limits	Items will not assess transformations beyond Clarification 1.
	Items may include the use of words or coordinate notation using
	algebraic descriptors for describing the transformation(s).
	Items should reference two different figures and are limited to a single
	transformation or a sequence of two to four transformations.
	Items may include rigid transformations of circles.

MA.912.GR.2	Apply properties of transformations to describe congruence or
	similarity.
MA.912.GR.2.5	Given a geometric figure and a sequence of transformations, draw the
	transformed figure on a coordinate plane.
Benchmark	Clarification 1: Transformations include translations, dilations, rotations
Clarifications	and reflections described using words or using coordinates.
	Clarification 2: Instruction includes two or more transformations.
Context	Mathematical
Calculator	Available
Assessment Limits	Items will not assess transformations beyond Clarification 1.
	Items are limited to a sequence of two to four transformations.
	Items may include the use of words or coordinate notation using
	algebraic descriptors for describing the transformations.
	Items may include identifying coordinate pairs of vertices of
	transformed figures.

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.
MA.912.GR.4.3	Extend previous understanding of scale drawings and scale factors to
	determine how dilations affect the area of two-dimensional figures and
	the surface area or volume of three-dimensional figures.
	<i>Example:</i> Mike is having a graduation party and wants to make sure he
	has enough pizza. Which option would provide more pizza for his
	guests: one 12-inch pizza or three 6-inch pizzas?
Context	Both
Calculator	Available
Assessment Limits	Items that require the student to find the volume or surface area of a
	dilated figure must give the volume or surface area of the original
	figure.

MA.912.GR.5	Make formal geometric constructions with a variety of tools and
	methods.
MA.912.GR.5.1	Construct a copy of a segment or an angle.
Benchmark	Clarification 1: Instruction includes using compass and straightedge,
Clarifications	string, reflective devices, paper folding or dynamic geometric software.
Context	Mathematical
Calculator	Available
Assessment Limits	Items will assess constructions through the use of compass and straight- edge with descriptions, images, and/or animations.
	Items must use straightedge and compass vocabulary when referencing tools.
	Items may ask the student to describe steps in a construction, identify the next step in a given construction, or describe what construction is being created.

MA.912.GR.5	Make formal geometric constructions with a variety of tools and methods.
MA.912.GR.5.2	Construct the bisector of a segment or an angle, including the perpendicular bisector of a line segment.
Benchmark	Clarification 1: Instruction includes using compass and straightedge,
Clarifications	string, reflective devices, paper folding or dynamic geometric software.
Context	Mathematical
Calculator	Available
Assessment Limits	<ul> <li>Items will assess constructions through the use of compass and straight- edge with descriptions, images, and/or animations.</li> <li>Items must use straightedge and compass vocabulary when referencing tools.</li> </ul>
	Items may ask the student to describe steps in a construction, identify the next step in a given construction, or describe what construction is being created.

MA.912.GR.5	Make formal geometric constructions with a variety of tools and
	methods.
MA.912.GR.5.3	Construct the inscribed and circumscribed circles of a triangle.
Benchmark	Clarification 1: Instruction includes using compass and straightedge,
Clarifications	string, reflective devices, paper folding or dynamic geometric software.
Context	Mathematical
Calculator	Available
Assessment Limits	<ul> <li>Items will assess constructions through the use of compass and straightedge with descriptions, images, and/or animations.</li> <li>Items may ask the student to describe steps in a construction, identify the next step in a given construction, or describe what construction is being created.</li> <li>Items may not refer to the orthocenter.</li> <li>Items must use straightedge and compass vocabulary when referencing tools.</li> </ul>

## **Measurement and Coordinate Geometry**

MA.912.GR.3	Use coordinate geometry to solve problems or prove relationships.
MA.912.GR.3.2	Given a mathematical or real-world context, use coordinate geometry to classify or justify definitions, properties and theorems involving circles, triangles or quadrilaterals. <i>Example:</i> Given Triangle ABC has vertices located at $(-2, 2)$ , $(3, 3)$ and $(1, -3)$ , respectively, classify the type of triangle ABC. <i>Example:</i> If a square has a diagonal with vertices $(-1, 1)$ and $(-4, -3)$ , find the coordinate values of the vertices of the other diagonal and show that the two diagonals are perpendicular.
Benchmark Clarifications	<i>Clarification 1:</i> Instruction includes using the distance or midpoint formulas and knowledge of slope to classify or justify definitions, properties and theorems.
Context	Both
Calculator	Available
Assessment Limits	N/A

MA.912.GR.3	Use coordinate geometry to solve problems or prove relationships.
MA.912.GR.3.3	Use coordinate geometry to solve mathematical and real-world
	geometric problems involving lines, circles, triangles and quadrilaterals.
	<i>Example</i> : The line $x + 2y = 10$ is tangent to a circle whose center is
	located at $(2, -1)$ . Find the tangent point and a second tangent point of
	a line with the same slope as the given line.
	<i>Example</i> : Given $M(-4, 7)$ and $N(12, -1)$ , find the coordinates of point
	<i>P</i> on $\overline{MN}$ so that <i>P</i> partitions $\overline{MN}$ in the ratio 2:3.
Benchmark	Clarification 1: Problems involving lines include the coordinates of a
Clarifications	point on a line segment including the midpoint.
	<i>Clarification 2:</i> Problems involving circles include determining points on
	a given circle and finding tangent lines.
	Clarification 3: Problems involving triangles include median and
	centroid.
	Clarification 4: Problems involving quadrilaterals include using parallel
	and perpendicular slope criteria.
Also Assesses	
MA.912.GR.3.1	Determine the weighted average of two or more points on a line.
Benchmark	<i>Clarification 1:</i> Instruction includes using a number line and determining
Clarifications	how changing the weights moves the weighted average of points on the
	number line.
Context	Both
Calculator	Available
Assessment Limits	Items will not assess beyond the Benchmark Clarifications.
	Items assessing MA.912.GR.3.1 must use only two points and either
	reference or be presented on a number line. Items assessing
	MA.912.GR.3.1 should have weights that total to 1 using fractions or
	percentages.
	Items may not refer to the orthocenter.

MA.912.GR.3	Use coordinate geometry to solve problems or prove relationships.
MA.912.GR.3.4	Use coordinate geometry to solve mathematical and real-world
	problems on the coordinate plane involving perimeter or area of
	polygons.
	<i>Example:</i> A new community garden has four corners. Starting at the first
	corner and working counterclockwise, the second corner is 200 feet
	east, the third corner is 150 feet north of the second corner and the
	fourth corner is 100 feet west of the third corner. Represent the garden
	in the coordinate plane, and determine how much fence is needed for
	the perimeter of the garden and determine the total area of the garden.
Context	Both
Calculator	Available
Assessment Limits	Items will require the student to find the length of at least one side that
	is not parallel to an axis.
	Items may use population density in solving problems.

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.				
MA.912.GR.4.1	Identify the shapes of two-dimensional cross-sections of three-				
	dimensional figures.				
Benchmark	<i>Clarification 1:</i> Instruction includes the use of manipulatives and models				
Clarifications	to visualize cross-sections.				
	Clarification 2: Instruction focuses on cross-sections of right cylinders,				
	right prisms, right pyramids and right cones that are parallel or				
	perpendicular to the base.				
Context	Both				
Calculator	Available				
Assessment Limits	Items are limited to the shapes and cross-sections listed in Clarification				
	2.				
	Items can include composite shapes composed of figures listed in				
	Clarification 2.				
	Items must use bases that are either a rectangle or a regular polygon for				
	right prisms and right pyramids.				
	Items assessing a cross-section perpendicular to the base of a cone and				
	not through the apex must use images for identifying the shape of				
	the cross-section.				

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.		
MA.912.GR.4.2	Identify three-dimensional objects generated by rotations of two-		
	dimensional figures.		
Benchmark	<i>Clarification 1:</i> The axis of rotation must be within the same plane but		
Clarifications	outside of the given two-dimensional figure.		
Context	Both		
Calculator	Available		
Assessment Limits	Items can include rotation about the side of the two-dimensional object.		
	Items can include composite shapes.		

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.		
MA.912.GR.4.4	Solve mathematical and real-world problems involving the area of two-		
	dimensional figures.		
	<i>Example</i> : A town has 23 city blocks, each of which has dimensions of 1		
	quarter mile by 1 quarter mile, and there are 4500 people in the town.		
	What is the population density of the town?		
Benchmark	Clarification 1: Instruction includes concepts of population density		
Clarifications	based on area.		
Context	Both		
Calculator	Available		
Assessment Limits	Items representing side lengths as expressions must result in a non-		
	linear equation.		
	Items with polygons should only include the radius and apothem or radius and side length.		

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.		
MA.912.GR.4.5	Solve mathematical and real-world problems involving the volume of		
	three-dimensional figures limited to cylinders, pyramids, prisms, cones		
	and spheres.		
	<i>Example</i> : A cylindrical swimming pool is filled with water and has a		
	diameter of 10 feet and height of 4 feet. If water weighs 62.4 pounds		
	per cubic foot, what is the total weight of the water in a full tank to the		
	nearest pound?		
Benchmark	Clarification 1: Instruction includes concepts of density based on		
Clarifications	volume.		
	Clarification 2: Instruction includes using Cavalieri's Principle to give		
	informal arguments about the formulas for the volumes of right and		
	non-right cylinders, pyramids, prisms and cones.		
Context	Both		
Calculator	Available		
Assessment Limits	Items can include composite or oblique figures.		

MA.912.GR.4	Use geometric measurement and dimensions to solve problems.			
MA.912.GR.4.6	Solve mathematical and real-world problems involving the surface area			
	of three-dimensional figures limited to cylinders, pyramids, prisms,			
	cones and spheres.			
Context	Both			
Calculator	Available			
Assessment Limits	Items can include composite figures.			
	Items will not include oblique figures.			

MA.912.GR.7	Apply geometric and algebraic representations of conic sections.		
MA.912.GR.7.2	Given a mathematical or real-world context, derive and create the		
	equation of a circle using key features.		
Benchmark	<i>Clarification 1:</i> Instruction includes using the Pythagorean Theorem and		
Clarifications	completing the square.		
	<i>Clarification 2:</i> Within the Geometry course, key features are limited to		
	the radius, diameter and the center.		
Context	Both		
Calculator	Available		
Assessment Limits	Items must give a graph or key features.		

MA.912.GR.7	Apply geometric and algebraic representations of conic sections.			
MA.912.GR.7.3	Graph and solve mathematical and real-world problems that are			
	modeled with an equation of a circle. Determine and interpret key			
	features in terms of the context.			
Benchmark	<i>Clarification 1:</i> Key features are limited to domain, range, eccentricity,			
Clarifications	center and radius.			
	Clarification 2: Instruction includes representing the domain and range			
	with inequality notation, interval notation or set-builder notation.			
	Clarification 3: Within the Geometry course, notations for domain and			
	range are limited to inequality and set-builder.			
Context	Both			
Calculator	Available			
Assessment Limits	Angle measures will be in degrees.			
	Items will not assess eccentricity.			
	Items must give the equation of the circle.			

MA.912.T.1	Define and use trigonometric ratios, identities or functions to solve problems.		
MA.912.T.1.2	Solve mathematical and real-world problems involving right triangles		
	using trigonometric ratios and the Pythagorean Theorem.		
Benchmark	Clarification 1: Instruction includes procedural fluency with the		
Clarifications	relationships of side lengths in special right triangles having angle		
	measures of 30°-60°-90° and 45°-45°-90°.		
Also Assesses			
MA.912.T.1.1	Define trigonometric ratios for acute angles in right triangles.		
Benchmark	Clarification 1: Instruction includes using the Pythagorean Theorem and		
Clarifications	using similar triangles to demonstrate that trigonometric ratios stay the		
	same for similar right triangles.		
	<i>Clarification 2:</i> Within the Geometry course, instruction includes using		
	the coordinate plane to make connections to the unit circle.		
	<i>Clarification 3:</i> Within the Geometry course, trigonometric ratios are		
	limited to sine, cosine and tangent.		
Context	Both		
Calculator	Available		
Assessment Limits	Items will not address connections to the unit circle.		
	Angle measures will be in degrees.		

Appendix A

### **B.E.S.T. Geometry EOC Mathematics Reference Sheet**

Customary	Metric Conversions	Time Conversions	
Conversions	1 meter = 100 centimeters	1 minute = 60 seconds	
1 foot = 12 inches 1 yard = 3 feet 1 mile = 5,280 feet 1 mile = 1,760 yards	1 meter = 1000 millimeters 1 kilometer = 1000 meters 1 liter = 1000 milliliters	1 hour = 60 minutes 1 day = 24 hours 1 year = 365 days 1 year = 52 weeks	
1 cup = 8 fluid ounces 1 pint = 2 cups 1 quart = 2 pints 1 gallon = 4 quarts	1 gram = 1000 milligrams 1 kilogram = 1000 grams		
1 pound = 16 ounces 1 ton = 2,000 pounds			

Distance Formula	Midpoint Formula	Slope Formula
$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$	$(x_M, y_M) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$	$m = \frac{y_2 - y_1}{x_2 - x_1}$



### **B.E.S.T. Geometry EOC Mathematics Reference Sheet**

### Formulas

Parallelogram	A = bh	]	Кеу	
	1	-	P = perimeter	A = area
Trapezoid	$A = \frac{1}{2}h(b_1 + b_2)$		a = apothem	C = circumference
	Ζ · · · ·		h = height	SA = surface area
	$C = 2\pi r \circ r C = \pi d$		r = radius	V = volume
Circle	$C = 2\pi i \text{ of } C = \pi u$		$h_s$ = slant height	
	$A = \pi r^2$		l = slant height	
Regular Polygon	1 - 1	1	b = base	
Regular i orygoli	$A = \frac{1}{2}Pu$		d = diameter	
			B = area of base	
Prism/Cylinder	SA = 2B + Ph			
i iisiii eyiinder	V = Bh			
	$SA = B + \pi r h_s$ or			
Cone	$SA = B + \pi r l$			
	$V = \frac{1}{3}Bh$			
	$SA = B + \frac{1}{2}Ph_s$ or			
Regular Pyramid	egular Pyramid $SA = B + \frac{1}{2}Pl$			
	$V = \frac{1}{3}Bh$			
Salvara	$SA = 4\pi r^2$	r		
Sphere	$V = \frac{4}{3}\pi r^3$			

Trigonometric Ratios			
$\sin \theta = \frac{opposite}{hypotenuse}$	$\cos\theta = \frac{adjacent}{hypotenuse}$	$\tan \theta = \frac{opposite}{adjacent}$	

Appendix B

Numeric Only								Full Keypad														
	$(\bullet, \bullet, \bullet, \bullet, \bullet)$																					
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### **Keypads for Geometry Computer-Based Tests**

Appendi	x C:	Change	Log
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Page(s)	Change	Date
Global	Reordered benchmarks according to reporting	November 2022
	categories	
20	Changed "Measurement and Geometry" to	November 2022
	"Measurement and Coordinate Geometry"	
1	Added "AND REVIEWERS" after "ITEM WRITERS"	June 2023
3	Removed "of" after "select all" in the multi-	June 2023
	select section.	
13	Corrected spelling of "assess" in assessment	June 2023
	limits	
17	Added assessment limit to 912.GR.2.5: Items	June 2023
	may include identifying coordinate pairs of	
	vertices of transformed figures.	
18-19	Updated assessment limit of 912.GR.5	June 2023
	benchmarks: Items must use straightedge and	
	compass vocabulary when referencing tools.	
19	Added assessment limit to 912.GR.5.3: Items	June 2023
	may not refer to the orthocenter.	
19	Deleted assessment limit: There was a repeat	June 2023
	assessment limit about straightedge and	
	compass vocabulary.	
21	Added assessment limit to 912.GR.3.3: Items	June 2023
	may not refer to the orthocenter.	
27	Corrected formatting so that each table aligns at	June 2023
	the top	
28	Added "the" after "same as" in Full Keypad With	June 2023
	Variables section. Added period to end of	
	statement.	
3-4	Updated language to remove "scanned and	August 2023
	scored electronically."	